

Augmenting Network Architectures and Loss Functions Using Logic Rules

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Overview

Tasks = contracts

We want models that do more than what the data says

Learning from ~~examples~~ Knowledge

Relaxing logic and using relaxed logic to learn

Three case studies

Augmentation

For natural language inference

Cnsistency

Structur**d**
Tuning for SRL

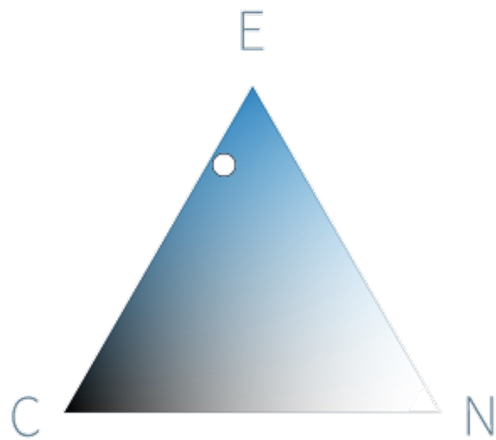
Tasks = contracts

We want models that do more than what the data says

Example 1: Natural language inference

Premise Before it moved to Chicago, aerospace manufacturer Boeing was the largest company in Seattle.

Hypothesis Boeing is a Chicago-based aerospace manufacturer.

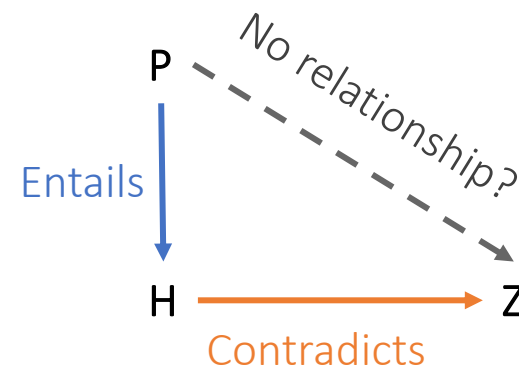


Judgment	Probability
Entailment	75.6%
Contradiction	19.9%
Neutral	4.5%

It is quite likely that the premise **entails** the hypothesis.

Can neural networks understand text?

- P John is on a train to Berlin.
- H John is traveling to Berlin.
- Z John is having lunch in Berlin.



The same system cannot simultaneously hold these three beliefs!

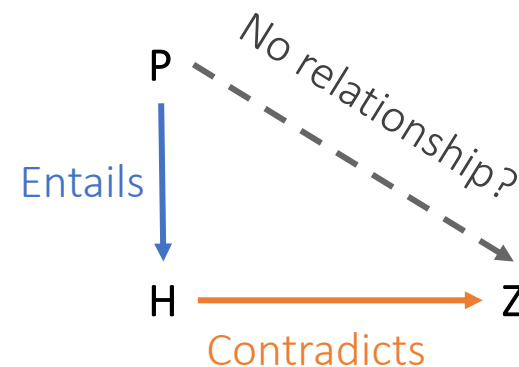
Violates this invariant

If *P entails H* and *H contradicts Z*,
then *P contradicts Z*

A BERT-based model that gets ~90% on benchmark data violates this invariant on 46% of a large collection of sentence triples.

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Violates this invariant

If *P entails H* and *H contradicts Z*

Can neural networks use such “theory” in the form of invariant knowledge?

A BERT-based model that gets ~90% on benchmark data violates this invariant on 46% of a large collection of sentence triples.

Tasks* define predicates

Example: The natural language inference task defines three predicates called **Entail** (P, H), **Contradict** (P, H) and **Neutral** (P, H)

P	John is on a train to Berlin.	→	Entail (P, H)
H	John is traveling to Berlin.		\neg Contradict (P, H) \neg Neutral (P, H)

Labeled datasets show examples of these predicates

Models try to find the best fitting predicates given their arguments

Model behavior as constraints

Expected behavior: *“If a sentence P entails a sentence H , and H entails the sentence Z , then P entails Z ”*

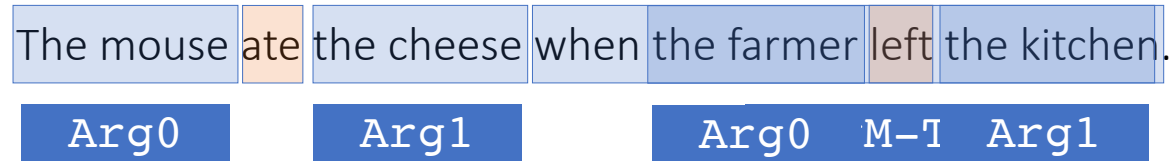
\forall sentences $P, H, Z,$ **Entail** $(P, H) \wedge$ **Entail** $(H, Z) \rightarrow$ **Entail** (P, Z)
(Four such valid transitivity constraints exist)

Expected behavior: *“The contradict predicate is symmetric.”*

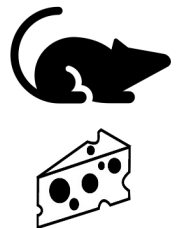
\forall sentences $P, H,$ **Contradict** $(P, H) \leftrightarrow$ **Contradict** (H, P)

Example 2: Semantic Role Labeling (SRL)

Who did what to whom, where, when, why?



These *semantic roles* are defined by the PropBank data (Palmer et al)



ate	
Arg0	The mouse
Arg1	the cheese
ArgM-TMP	when the farmer left the kitchen

left	
Arg0	the farmer
Arg1	the kitchen



Semantic Role Labeling: The contract

- **Input:** A sentence
- **Output:** *Structured* semantic frames for all verbs

Expected behavior: Outputs should satisfy certain constraints

- Core arguments (e.g. **Arg0**, **Arg1**) cannot repeat...
...but modifiers (e.g. **ArgM-TMP**) can
- Certain arguments (called references, e.g. **R-Arg0**) can appear only if the corresponding referent argument exists (here, **Arg0**)

*These **symbolic** constraints come from the task definition and linguistic assumptions*

If labels satisfy symbolic properties...

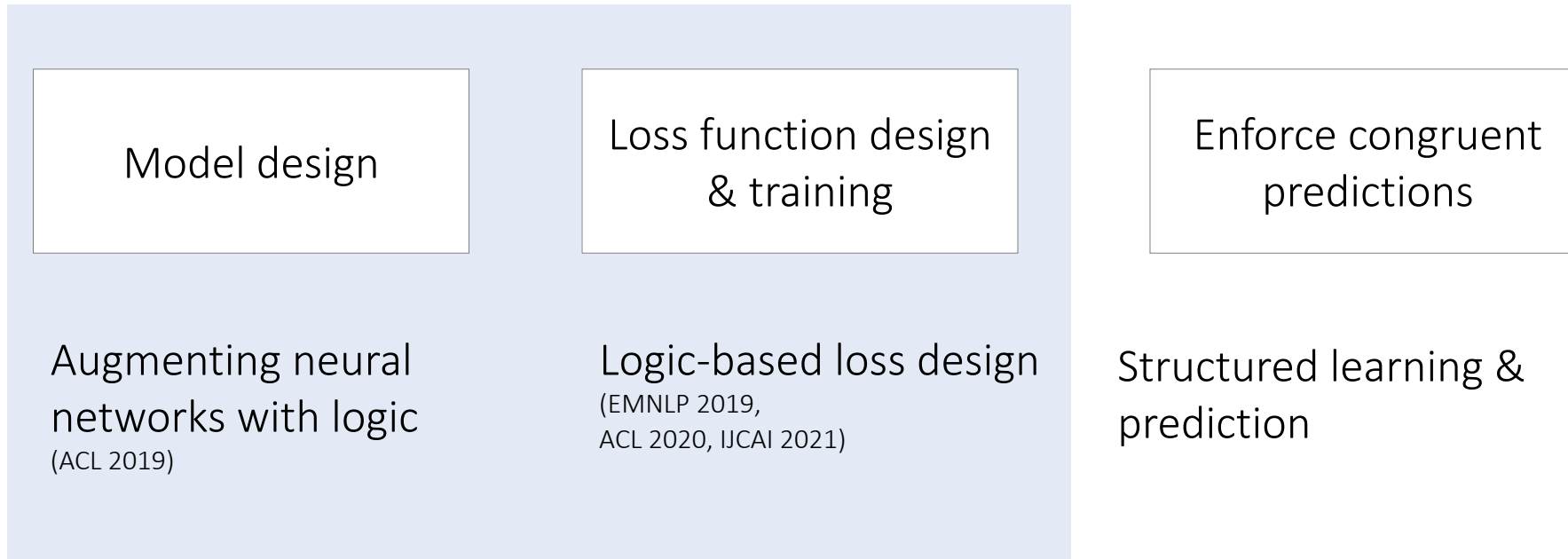
...when and how do we inject this knowledge into the modeling and prediction process?

Can we do so using the existing gradient-based machinery for neural networks?

Learning from ^{knowledge}~~examples~~

Relaxing logic and using relaxed logic to learn

Where can knowledge be involved?



This section of the tutorial

Neural network land vs. Logic land

Neural Networks

✓ Differentiable compute, easy to use

✗ Hard to supervise except via labeled examples

First-order logic

✗ Not differentiable, hard to use with today's best infrastructure

✓ Expressive and easy to state for domain experts

What we want: **Best of both!**

Three challenges facing logic in neural network land

1. Bridging predicates in rules with neural networks
2. Making logic differentiable
3. Using differentiable logic

Predicates in neural networks

All neural networks expose *interfaces* in the form of nodes that have externally defined meaning

Recall: Labels are predicates

P John is on a train to Berlin.

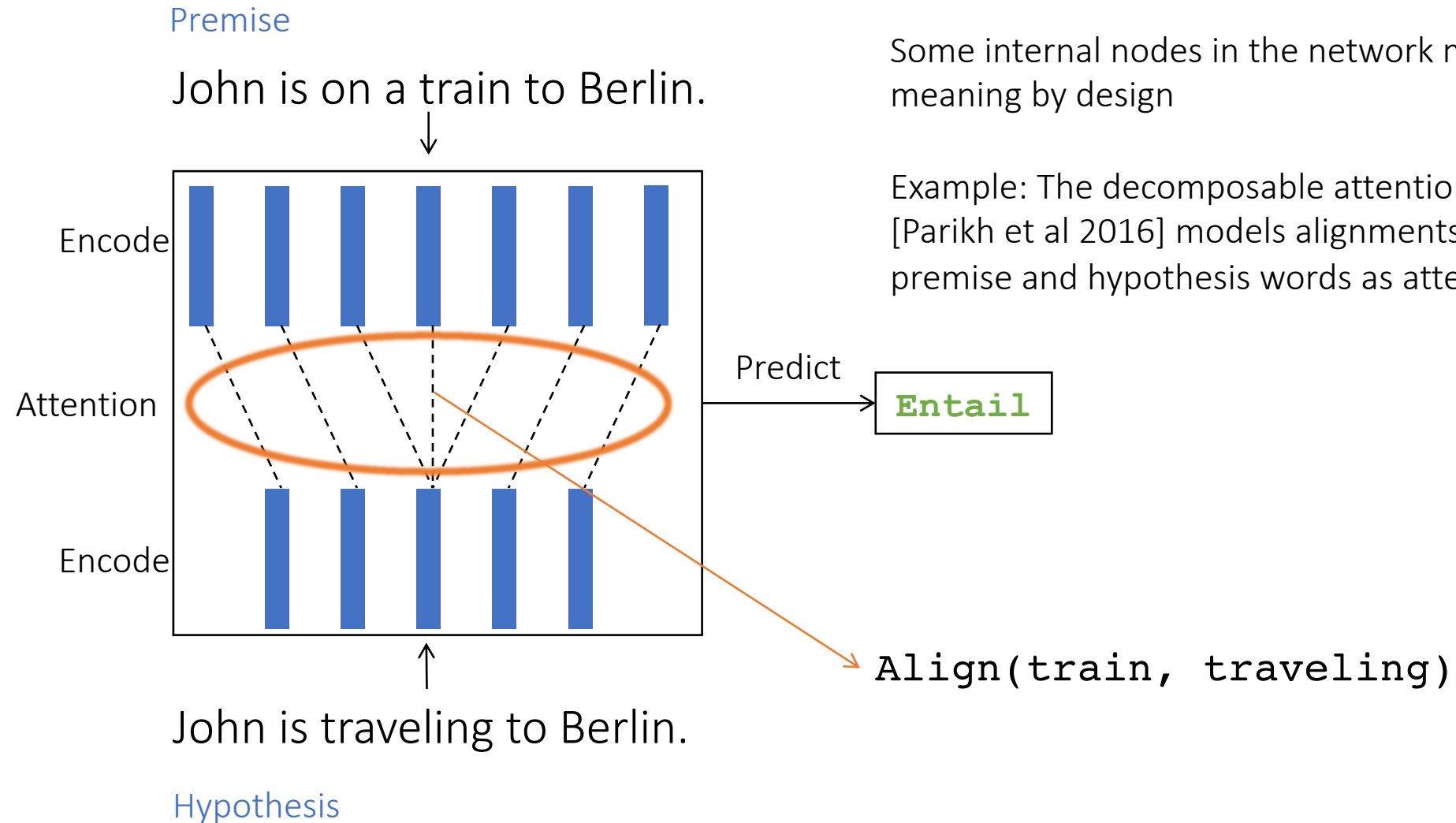
H John is traveling to Berlin.



Labeled datasets are formal specifications

$$\begin{aligned} & (P1, H1, \text{Entail}) \\ & (P2, H2, \text{Contradict}) \\ & (P3, H3, \text{Neutral}) \\ & (P4, H4, \text{Neutral}) \end{aligned} = \begin{aligned} & \text{Entail}(P1, H1) \\ & \wedge \text{Contradict}(P2, H2) \\ & \wedge \text{Neutral}(P3, H3) \\ & \wedge \text{Neutral}(P4, H4) \end{aligned}$$

Predicates *within* neural networks



Named neurons

Nodes in a computation graph that have *externally* defined meaning

Named neurons can be:

- Any output nodes in the network
- Inputs to the network and their deterministic properties
- Sometimes, internal nodes that have defined behavior

Named neurons give us the vocabulary for writing rules

Three challenges facing logic in neural network land

1. Bridging predicates in rules with neural networks?

Answer: Named neurons, nodes in a computation graph that have externally defined meaning

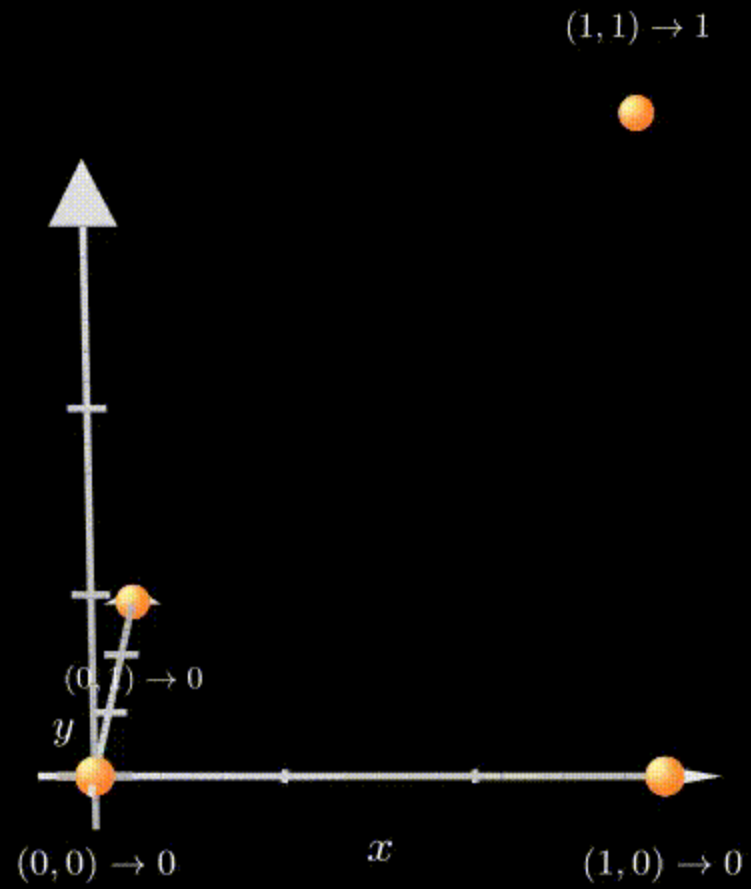
2. Making logic differentiable?
3. Using differentiable logic?

Relaxing Boolean operators

Triangular norms provide systematic relaxations of logic

Some are continuous and sub-differentiable

Inputs, outputs live in $\{0,1\}$	
Boolean logic	
Not	$\neg A$
And	$A \wedge B$
Or	$A \vee B$
Implies	$A \rightarrow B$



Relaxing Boolean operators

Triangular norms provide systematic relaxations of logic

Some are continuous and sub-differentiable

Inputs, outputs live in $\{0,1\}$		Inputs, outputs live in $[0,1]$		
	Boolean logic	Product	Gödel	Łukasiewicz
Not	$\neg A$	$1 - a$	$1 - a$	$1 - a$
And	$A \wedge B$	ab	$\min(a, b)$	$\max(0, a + b - 1)$
Or	$A \vee B$	$a + b - ab$	$\max(a, b)$	$\min(1, a + b)$
Implies	$A \rightarrow B$	$\min\left(1, \frac{b}{a}\right)$	$\begin{cases} 1 & \text{if } b > a \\ b & \text{else} \end{cases}$	$\min(1, 1 - a + b)$

Three challenges facing logic in neural network land

1. Bridging predicates in rules with neural networks?

Answer: Named neurons, nodes in a computation graph that have externally defined meaning

2. Making logic differentiable?

Answer: Use a t-norm relaxation

3. Using differentiable logic?

What logic can do for neural networks?

Introduce inductive bias by...

- ...changing network architecture
to networks that prefer satisfying the constraints
- ...by regularizing learning
to penalize models that violate the constraints

What logic can do for neural networks?

Introduce inductive bias by...

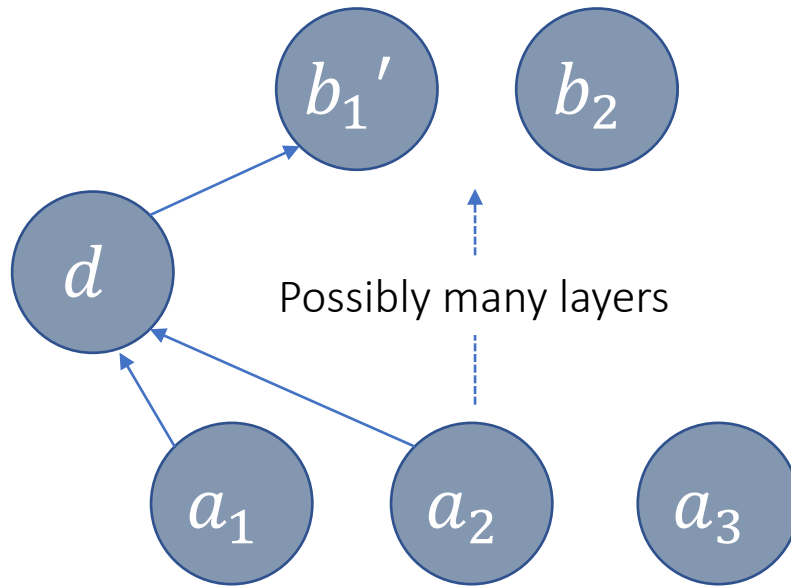
- ...changing network architecture
to networks that prefer satisfying the constraints
- ...by regularizing learning
to penalize models that violate the constraints

Augmenting models: An example

$$b_1' = \sigma(\mathbf{w}^T \mathbf{x} + \rho d(a_1, a_2))$$

$$\cancel{b_1 = \sigma(\mathbf{w}^T \mathbf{x})}$$

$$A_1 \wedge A_2 \rightarrow B_1$$



Step 1: LHS in Łukasiewicz logic

$$d(a_1, a_2) = \max(0, a_1 + a_2 - 1)$$

Step 2: Define constrained node b_1'

Step 3: Replace original b_1 with b_1'

No additional trainable parameters introduced

Hyperparameter ρ controls how strongly the constraint is enforced

What logic can do for neural networks?

Introduce inductive bias by...

- ...changing network architecture
to networks that prefer satisfying the constraints
- ...by regularizing learning
to penalize models that violate the constraints

Unifying data & knowledge

Labeled data = propositions about examples

Knowledge can be written as rules

- e.g. $\forall P, H, Z, \text{Entail}(P, H) \wedge \text{Entail}(H, Z) \rightarrow \text{Entail}(P, Z)$
- Universally quantified

Labeled examples and constraints are, together, a collection of rules of the form

$$\forall x, L(x) \rightarrow R(x)$$

Encouraging consistency of models

$$\forall x, L(x) \rightarrow R(x)$$

Labeled data + knowledge

Learning goal: Prefer models that set all the rules of this form to be true

Or alternatively: Find models maximize a t-norm relaxation

Inconsistency losses

Use any neural model, any library and any optimizer
Product t-norm + labeled examples gives cross entropy loss

Case studies

Natural Language Inference

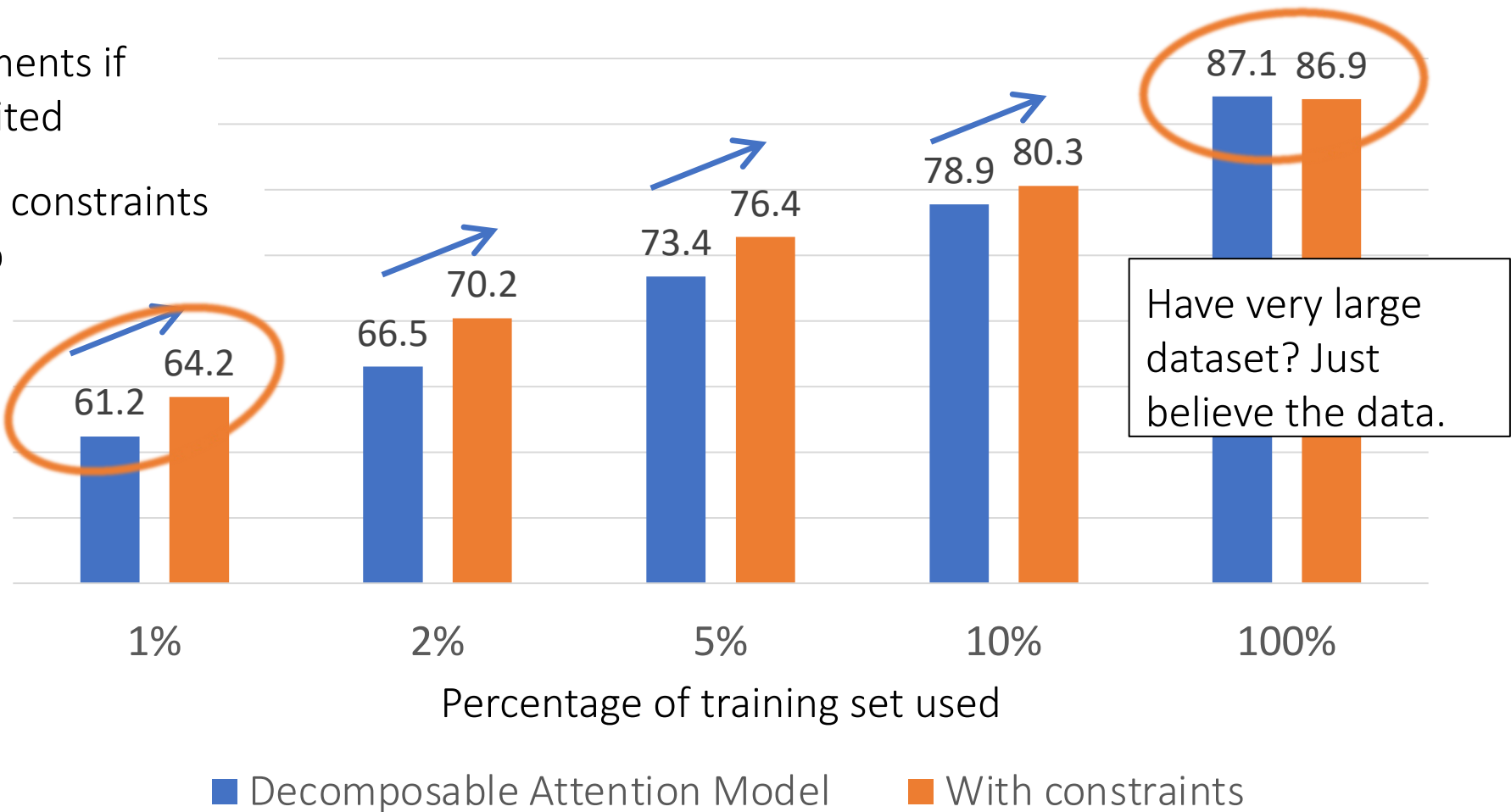
SNLI dataset, decomposable attention model [Parikh et al 2016]

Two constraints (written in logic):

1. If two words are related, they should be aligned
2. If no content word in the hypothesis is aligned,
then the label cannot be **Entail**

Results: Natural Language Inference

- 1. Constraints help
- 2. Larger improvements if training data is limited
- 3. With 0.5M data, constraints don't seem to help



Inconsistency of natural language inference

BERT based models for SNLI & MultiNLI datasets

Two kinds of regularizers from constraints:

1. Symmetry constraint:

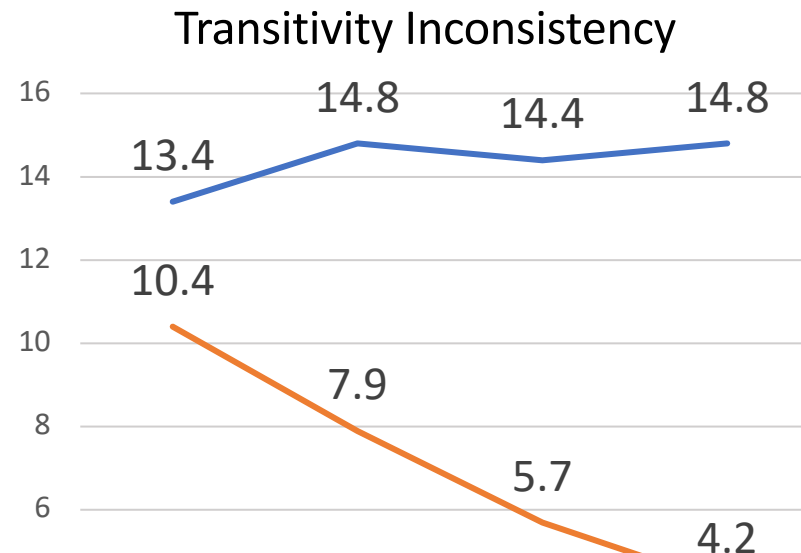
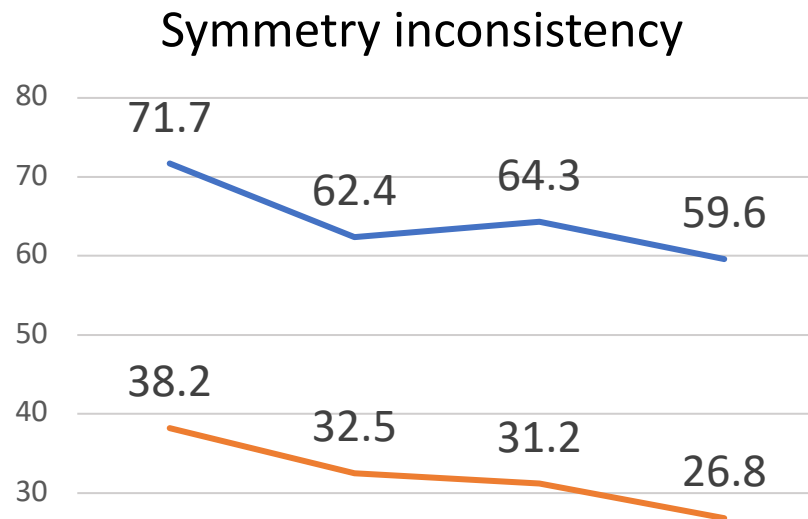
$$\forall P, H, \text{Contradict}(P, H) \leftrightarrow \text{Contradict}(H, P)$$

2. Four transitivity constraints of the form

$$\text{Entail}(P, H) \wedge \text{Entail}(H, Z) \rightarrow \text{Entail}(P, Z)$$

Results: Inconsistency of natural language inference

Inconsistency represents violation of constraints. Lower is better.



1. Merely adding more data does not make models consistent
2. Logic-based regularizers help with consistency

1% 5% 10% 100%

— BERT — With regularizer

1% 5% 20% 100%

— BERT — With regularizer

Constraints in SRL: Unique Core Roles

Each core argument can occur at most once in the output for a verb

For any verb u , and a word i for any core argument X (i.e. one of **A0**, **A1**, **A2**, **A3**, **A4**, **A5**)

If a model labels the i^{th} word as the beginning of a label X

Then, for any other word j \Rightarrow model cannot predict that it is the beginning of the same label

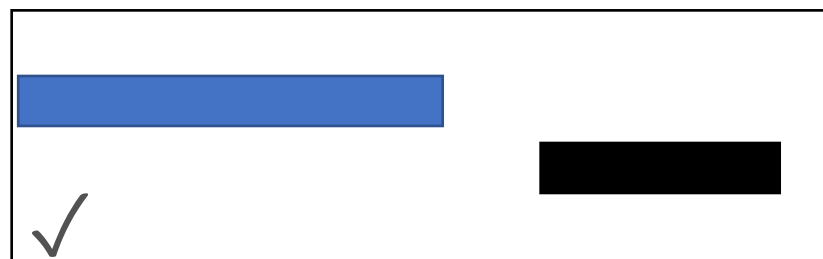
1. Compile into a differentiable expression using a t-norm
2. Minimize the negative of the expression as part of training

Other constraints (informally)

Both compiled to losses

The exclusively overlapping role constraint:

- In any sentence, an argument for a predicate can either be contained in, or fully outside, the argument for any predicate



The frame core role constraint

- A verb can have only those core arguments that are defined in PropBank

Scenario 1: The low data regime

- Train with 3% data with and without constraints
 - CoNLL 05: 1.1k examples
 - CoNLL 12: 2.7k examples
- Constraints greatly improve precision in the low data regime over the strong RoBERTa baseline
 - CoNLL 05: 70.48 → 72.6
 - CoNLL 12: 74.79 → 76.31
 - F-scores also improve (paper has details)
- Constraint violations reduced, especially for unique core roles and the frame constraints

Scenario 2: More training data

- Train with the full CoNLL 05 data
- Surprisingly still better in terms of precision, recall and f-scores, though the margin is lower
 - Strong out of domain performance on Brown corpus data
- Constraint violations reduced for unique core roles and the frame constraints
 - The unconstrained model doesn't seem to violate the exclusive overlap constraint!

CoNLL 05: 35k examples,
91k propositions

Test f-score: 87.85 → 88.03
Brown f-score: 78.64 → 79.80

Scenario 3: Even more training data

- Train with the full CoNLL 12 data
- Constrained and unconstrained models are comparable

CoNLL 05: 90k examples,
253k propositions

Test f-score: 86.47 → 86.61

If you have a lot of data, it is okay to believe the data

Knowledge via soft logic helps neural models

Successful experiments across many different tasks

- Natural language inference
- Question answering
- Text chunking
- Semantic role labeling
- Joint digit recognition and numerical operations over them
- Information extraction

Thanks!
Questions?

General flavor of results

1. When we have less data, knowledge gives better statistical models
2. We can “inject” invariances into learned systems...
...which are sometimes not learned, even with lots of data